

# Markscheme

# May 2019

# **Mathematics**

**Higher level** 

Paper 2

**(b**)

18 pages

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#### Instructions to Examiners

- 3 -

#### Abbreviations

- *M* Marks awarded for attempting to use a valid **Method**; working must be seen.
- (M) Marks awarded for **Method**; may be implied by **correct** subsequent working.
- **A** Marks awarded for an **Answer** or for **Accuracy**; often dependent on preceding **M** marks.
- (A) Marks awarded for an Answer or for Accuracy; may be implied by correct subsequent working.
- *R* Marks awarded for clear **Reasoning**.
- *N* Marks awarded for **correct** answers if **no** working shown.
- **AG** Answer given in the question and so no marks are awarded.

#### Using the markscheme

#### 1 General

Mark according to RM<sup>™</sup> Assessor instructions. In particular, please note the following:

- Marks must be recorded using the annotation stamps. Please check that you are entering marks for the right question.
- If a part is **completely correct**, (and gains all the "must be seen" marks), use the ticks with numbers to stamp full marks.
- If a part is completely wrong, stamp **A0** by the final answer.
- If a part gains anything else, it **must** be recorded using **all** the annotations.
- All the marks will be added and recorded by RM<sup>™</sup> Assessor.

#### 2 Method and Answer/Accuracy marks

- Do **not** automatically award full marks for a correct answer; all working **must** be checked, and marks awarded according to the markscheme.
- It is not possible to award *M0* followed by *A1*, as *A* mark(s) depend on the preceding *M* mark(s), if any.
- Where *M* and *A* marks are noted on the same line, *eg M1A1*, this usually means *M1* for an **attempt** to use an appropriate method (*eg* substitution into a formula) and *A1* for using the **correct** values.
- Where the markscheme specifies (M2), N3, etc., do not split the marks.

 Once a correct answer to a question or part-question is seen, ignore further correct working. However, if further working indicates a lack of mathematical understanding do not award the final *A1*. An exception to this may be in numerical answers, where a correct exact value is followed by an incorrect decimal. However, if the incorrect decimal is carried through to a subsequent part, and correct *FT* working shown, award *FT* marks as appropriate but do not award the final *A1* in that part.

#### Examples

	Correct answer seen	Further working seen	Action
1.	$8\sqrt{2}$	5.65685 (incorrect decimal value)	Award the final <b>A1</b> (ignore the further working)
2.	$\frac{1}{4}\sin 4x$	$\sin x$	Do not award the final <b>A1</b>
3.	$\log a - \log b$	$\log(a-b)$	Do not award the final <b>A1</b>

#### 3 N marks

Award **N** marks for **correct** answers where there is **no** working.

- Do **not** award a mixture of **N** and other marks.
- There may be fewer **N** marks available than the total of **M**, **A** and **R** marks; this is deliberate as it penalizes candidates for not following the instruction to show their working.

#### 4 Implied marks

Implied marks appear in **brackets eg (M1)**, and can only be awarded if **correct** work is seen or if implied in subsequent working.

- Normally the correct work is seen or implied in the next line.
- Marks without brackets can only be awarded for work that is seen.

#### 5 Follow through marks

Follow through (**FT**) marks are awarded where an incorrect answer from one **part** of a question is used correctly in **subsequent** part(s). To award **FT** marks, **there must be working present** and not just a final answer based on an incorrect answer to a previous part.

- If the question becomes much simpler because of an error then use discretion to award fewer *FT* marks.
- If the error leads to an inappropriate value (eg  $\sin \theta = 1.5$ ), do not award the mark(s) for the final answer(s).
- Within a question part, once an error is made, no further **dependent** *A* marks can be awarded, but *M* marks may be awarded if appropriate.
- Exceptions to this rule will be explicitly noted on the markscheme.

#### 6 Misread

If a candidate incorrectly copies information from the question, this is a misread (**MR**). A candidate should be penalized only once for a particular misread. Use the **MR** stamp to indicate that this has been a misread. Then deduct the first of the marks to be awarded, even if this is an **M** mark, but award all others so that the candidate only loses **[1 mark]**.

- 5 -

- If the question becomes much simpler because of the *MR*, then use discretion to award fewer marks.
- If the *MR* leads to an inappropriate value ( $eg \sin \theta = 1.5$ ), do not award the mark(s) for the final answer(s).

#### 7 Discretionary marks (d)

An examiner uses discretion to award a mark on the rare occasions when the markscheme does not cover the work seen. In such cases the annotation DM should be used and a brief **note** written next to the mark explaining this decision.

#### 8 Alternative methods

Candidates will sometimes use methods other than those in the markscheme. Unless the question specifies a method, other correct methods should be marked in line with the markscheme. If in doubt, contact your team leader for advice.

- Alternative methods for complete questions are indicated by METHOD 1, METHOD 2, etc.
- Alternative solutions for part-questions are indicated by EITHER . . . OR.
- Where possible, alignment will also be used to assist examiners in identifying where these alternatives start and finish.

#### 9 Alternative forms

Unless the question specifies otherwise, *accept* equivalent forms.

- As this is an international examination, accept all alternative forms of **notation**.
- In the markscheme, equivalent **numerical** and **algebraic** forms will generally be written in brackets immediately following the answer.
- In the markscheme, **simplified** answers, (which candidates often do not write in examinations), will generally appear in brackets. Marks should be awarded for either the form preceding the bracket or the form in brackets (if it is seen).

**Example**: for differentiating  $f(x) = 2\sin(5x-3)$ , the markscheme gives

$$f'(x) = (2\cos(5x-3))5 \ (=10\cos(5x-3))$$
 A1

Award **A1** for  $(2\cos(5x-3))5$ , even if  $10\cos(5x-3)$  is not seen.

# 10 Accuracy of Answers

Candidates should **NO LONGER** be penalized for an accuracy error (AP).

If the level of accuracy is specified in the question, a mark will be allocated for giving the answer to the required accuracy. When this is not specified in the question, all numerical answers should be given exactly or correct to three significant figures. Please check work carefully for **FT**.

# 11 Crossed out work

If a candidate has drawn a line through work on their examination script, or in some other way crossed out their work, do not award any marks for that work.

# 12 Calculators

A GDC is required for paper 2, but calculators with symbolic manipulation features (for example, TI-89) are not allowed.

### **Calculator notation**

The Mathematics HL guide says:

Students must always use correct mathematical notation, not calculator notation.

Do **not** accept final answers written using calculator notation. However, do not penalize the use of calculator notation in the working.

# 13 More than one solution

Where a candidate offers two or more different answers to the same question, an examiner should only mark the first response unless the candidate indicates otherwise.

# 14. Candidate work

Candidates are meant to write their answers to Section A on the question paper (QP), and Section B on answer booklets. Sometimes, they need more room for Section A, and use the booklet (and often comment to this effect on the QP), or write outside the box. This work should be marked.

The instructions tell candidates not to write on Section B of the QP. Thus they may well have done some rough work here which they assume will be ignored. If they have solutions on the answer booklets, there is no need to look at the QP. However, if there are whole questions or whole part solutions missing on answer booklets, please check to make sure that they are not on the QP, and if they are, mark those whole questions or whole part solutions that have not been written on answer booklets.

# Section A

1.	attempt to apply cosine rule	M1
	$\cos \mathbf{A} = \frac{5^2 + 11^2 - 14^2}{2 \times 5 \times 11} = -0.4545$	
	$\Rightarrow$ A = 117.03569°	
	$\Rightarrow A = 117.0^{\circ}$	A1
	attempt to apply sine rule or cosine rule:	M1
	sin117.03569° _ sin B	
	$\Rightarrow$ B = 44.4153°	
	$\Rightarrow$ B = 44.4°	A1
	$C = 180^{\circ} - A - B$	
	$C = 18.5^{\circ}$	A1
Not	e: Candidates may attempt to find angles in any order of their choosing.	

[5 marks]

	$\Rightarrow$ P(X > 1000) = 0.217	A1
		[2 n
(b)	$Y \sim B(24, 0.217)$	(M1)
Note	: Award <b>M1</b> for recognition of binomial distribution with parameters	S.
	$\mathbf{P}(Y \le 10) - \mathbf{P}(Y \le 4)$	(M1)
Note	: Award <b>M1</b> for an attempt to find $P(5 \le Y \le 10)$ or $P(Y \le 10) - P(Y \le 10)$	∕≤4).

Total [5 marks]

**3**. (a)



A1A1A1

**Note:** Award **A1** for each correct column of probabilities.

[3 marks]

(b) probability (at least twice) =

### EITHER

$$(0.6 \times 0.7 \times 0.8) + (0.6 \times 0.7 \times 0.2) + (0.6 \times 0.3 \times 0.6) + (0.4 \times 0.6 \times 0.7)$$
(M1)

OR

$$(0.6 \times 0.7) + (0.6 \times 0.3 \times 0.6) + (0.4 \times 0.6 \times 0.7)$$
 (M1)

Note: Award *M1* for summing all required probabilities. THEN

$$= 0.696$$

A1 [2 marks]

(c) P(passes third paper given only one paper passed before)  

$$= \frac{P (passes third AND only one paper passed before)}{P (passes once in first two papers)}$$

$$= \frac{(0.6 \times 0.3 \times 0.6) + (0.4 \times 0.6 \times 0.7)}{(0.6 \times 0.3) + (0.4 \times 0.6)}$$

$$= 0.657$$
A1  
[3 marks]

Total [8 marks]



Note: Accept x < 7.31.

[4 marks]

Total [6 marks]

A1

AG

[4 marks]

### 5. (a) **METHOD 1**

LHS = 
$$\frac{1 + \sin 2x}{\cos 2x} = \frac{1 + 2\sin x \cos x}{\cos^2 x - \sin^2 x}$$
 M1  
=  $\frac{(\cos^2 x + \sin^2 x) + 2\sin x \cos x}{\cos^2 x - \sin^2 x}$  M1

– 10 –

$$=\frac{\left(\cos x + \sin x\right)^{2}}{\left(\cos x + \sin x\right)\left(\cos x - \sin x\right)}$$
A1

$$= \frac{\frac{\cos x + \sin x}{\cos x - \sin x}}{\frac{\cos x}{\cos x} + \frac{\sin x}{\cos x}}$$
$$= \frac{\frac{\cos x}{\cos x} - \frac{\sin x}{\cos x}}{\frac{\cos x}{\cos x} - \frac{\sin x}{\cos x}}$$

 $=\frac{1+\tan x}{1-\tan x}$ 

Note: Candidates may start with RHS, apply MS in reverse.

#### **METHOD 2**

M1
M1
A1
۸1
AI

$$=\frac{1+\tan x}{1-\tan x}$$

**Note:** Candidates may start with RHS; apply MS in reverse.

[4 marks]

(b) valid attempt to solve 
$$\frac{1 + \tan x}{1 - \tan x} = \sqrt{3}$$
 (M1)  
 $\tan x = \frac{\sqrt{3} - 1}{\sqrt{3} + 1}$   
 $x = 0.262 \left( = \frac{\pi}{12} \right), x = 3.40 \left( = \frac{13\pi}{12} \right)$  A1  
Note: Award M1A0 if only one correct solution is given.

[2 marks]

Total [6 marks]

М1

(M1)

(M1)

A1

**6.** attempt to integrate a to find V

$$v = \int a \, dt = \int (2t-1) \, dt$$
  
=  $t^2 - t + c$   
$$s = \int v \, dt = \int (t^2 - t + c) \, dt$$

$$=\frac{t^3}{3}-\frac{t^2}{2}+ct+d$$
 **A1**

attempt at substitution of given values at t=6, 18.25 = 72 - 18 + 6c + dat t=15, 922.75 = 1125 - 112.5 + 15c + dsolve simultaneously: c = -6; d = 0.25 $\Rightarrow s = \frac{t^3}{3} - \frac{t^2}{2} - 6t + \frac{1}{4}$ 

[6 marks]

7.  $n=1 \Longrightarrow S_1 = u_1$ , so true for n=1

assume true for 
$$n = k$$
, ie.  $S_k = \frac{u_1(1-r^k)}{1-r}$ 

#### **Note:** Award *M0* for statements such as "let n = k".

Note: Subsequent marks after the first M1 are independent of this mark and can be awarded.

$$S_{k+1} = S_k + u_1 r^k$$
 M1

$$S_{k+1} = \frac{u_1(1-r^k)}{1-r} + u_1 r^k$$
(1)

$$S_{k+1} = \frac{u_1(1-r^k)}{1-r} + \frac{u_1r^k(1-r)}{1-r}$$

$$S_{k+1} = \frac{u_1 - u_1r^k + u_1r^k - ru_1r^k}{1-r}$$
A1

$$S_{k+1} = \frac{u_1(1 - r^{k+1})}{1 - r}$$

true for n = 1 and if true for n = k then true for n = k + 1 ,

#### Note: Award the final R1 mark provided at least four of the previous marks are gained.

[7 marks]

**R1** 

#### 8. (a) METHOD 1

$$w^{3} = 8i$$
writing  $8i = 8\left(\cos\left(\frac{\pi}{2} + 2\pi k\right) + i\sin\left(\frac{\pi}{2} + 2\pi k\right)\right)$ 
(M1)

Note: Award *M1* for an attempt to find cube roots of *w* using modulus-argument form.

cube roots 
$$w = 2\left(\cos\left(\frac{\frac{\pi}{2} + 2\pi k}{3}\right) + i\sin\left(\frac{\frac{\pi}{2} + 2\pi k}{3}\right)\right)$$
 (M1)

ie. 
$$w = \sqrt{3} + i, -\sqrt{3} + i, -2i$$
 **A2**

Note: Award A2 for all 3 correct, A1 for 2 correct.

**Note:** Accept w = 1.73 + i and w = -1.73 + i.

#### **METHOD 2**

 $w^{3} + (2i)^{3} = 0$ (w+2i)( $w^{2} - 2wi - 4$ ) = 0 M1

$$w = \sqrt{3} + i, -\sqrt{3} + i, -2i$$
Note: Award A2 for all 3 correct, A1 for 2 correct.
A2

**Note:** Accept w = 1.73 + i and w = -1.73 + i.

[4 marks]

(b) 
$$w_1 = -2i$$
  
 $\frac{z}{z-i} = -2i$   
 $z = -2i(z-i)$   
 $z(1+2i) = -2$   
 $z = \frac{-2}{1+2i}$   
 $z = -\frac{2}{5} + \frac{4}{5}i$   
A1

**Note:** Accept  $a = -\frac{2}{5}, b = \frac{4}{5}$ .

[3 marks]

Total [7 marks]

# Section B

9.	(a)	METHOD 1	
		attempt to find roots or factors	(M1)
		roots are $-3, 1, (4+i), (4-i)$	A1A1
	No	te: Award A1 for each pair of roots or factors, real and complex.	
		attempt to form quadratic	M1
		$(z-1)(z+3) = z^2 + 2z - 3$	A1
		(z - (4 + i))(z - (4 - i))	
		$= z^{2} - (4 - i)z - (4 + i)z + 17$	(A1)
		$= z^2 - 8z + 17$	A1
		$z^{4}-6z^{3}-2z^{2}+58z-51 = (z^{2}-8z+17)(z^{2}+2z-3)$	

#### **METHOD 2**

attempt to find roots or factors	(M1)
real roots are $-3$ , 1 (or real factors $(z + 3), (z - 1)$ )	A1
attempt to form quadratic	М1
$(z-1)(z+3) = z^2 + 2z - 3$	A1
$z^{4} - 6z^{3} - 2z^{2} + 58z - 51 = \left[z^{2} + 2z - 3\right]\left[z^{2} + kz + 17\right]$	
equate coefficients of $z^2$	М1
-2 = 2k - 3 + 17	A1
solve to give $k = -8$	A1
$z^{4}-6z^{3}-2z^{2}+58z-51 = (z^{2}-8z+17)(z^{2}+2z-3)$	

# [7 marks]

[7 marks]

#### **Question 9 continued**

(b)



 $P(X=0) = 0.122 (= e^{-2.1})$ 

(M1)A1

# [2 marks]

#### Question 10 continued

(b)

У	0	1	2	3	4
$\mathbf{P}(Y=y)$	0.122	0.257	0.270	0.189	0.161
	$\left(=e^{-2.1}\right)$	$(=e^{-2.1}2.1)$	$\left(=\frac{e^{-2.1}2.1^2}{2!}\right)$	$\left(=\frac{\mathrm{e}^{-2.1}2.1^3}{3!}\right)$	
					A1A1A1

<b>Note:</b> Award <b>A1</b> for each correct probability for $Y = 1, 2, 3, 4$ . Accept 0.162 for $P(Y = 4)$ .
--

(c) 
$$E(Y) = \sum y P(Y = y)$$
 (M1)  
= 1×0.257...+2×0.270...+3×0.189...+4×0.161...  
= 2.01 A1  
[3 marks]

(d)	let $T$ be the no of days per year that Steffi does not visit		
	$T \sim B(365, 0.122)$	(M1)	
	require $0.45 \le P(T \le n) < 0.55$	(M1)	
	$P(T \le 44) = 0.51$		
	n = 44	A1	
			[3 marks]

#### (e) METHOD 1

let $V$ be the discrete random variable "number of times Steffi is not fed per $Q$	day"
$E(V) = 1 \times P(X = 5) + 2 \times P(X = 6) + 3 \times P(X = 7) + \cdots$	M1
$= 1 \times 0.0416 + 2 \times 0.0145 + 3 \times 0.00437 + \cdots$	A1
= 0.083979	A1
expected no of occasions per year $> 0.083979 \times 365 = 30.7$	A1
hence Steffi can expect not to be fed on at least 30 occasions	AG

**Note:** Candidates may consider summing more than three terms in their calculation for E(V).

[4 marks]

#### **METHOD 2**

E(X) - E(Y) = 0.0903	M1A1
0.0903 × 365	M1
= 33.0 > 30	A1AG
	[4 marks]
	Total [16 marks]

11. (a) METHOD 1

for example

$$\vec{PQ} = \begin{pmatrix} -1 \\ -5 \\ 8 \end{pmatrix}, \vec{PR} = \begin{pmatrix} 1 \\ -6 \\ 3 \end{pmatrix}$$
 A1A1

$$\vec{PQ} \times \vec{PR} = 33i + 11j + 11k$$
(M1)A1
  
rn=an
(M2)

$$33x + 11y + 11z = \begin{pmatrix} 0\\1\\1 \end{pmatrix} \cdot \begin{pmatrix} 33\\11\\11 \end{pmatrix} = 22$$
(M1)

$$\Rightarrow 3x + y + z = 2 \text{ or equivalent}$$
 **A1**

[6 marks]

#### **METHOD 2**

assume plane can be written as ax + by + cz = 1substituting each set of coordinates gives the system of equations: a + 6b - 7c = 1 0a + b + c = 1 2a + 0b - 4c = 1solving by GDC (M1)  $a = \frac{3}{2}, b = \frac{1}{2}, c = \frac{1}{2}$  $\Rightarrow \frac{3}{2}x + \frac{1}{2}y + \frac{1}{2}z = 1$  or equivalent

[6 marks]

M1

#### (b) METHOD 1

substitution of equation of line into both equations of planes

$$3\left(\frac{5}{4}+\frac{\lambda}{2}\right)+\lambda+\left(-\frac{7}{4}-\frac{5\lambda}{2}\right)=2$$

$$\left(\frac{5}{4}+\frac{\lambda}{2}\right)-3\lambda-\left(-\frac{7}{4}-\frac{5\lambda}{2}\right)=3$$
A1

$$\left(\frac{1}{4} + \frac{1}{2}\right) - 3\lambda - \left(-\frac{1}{4} - \frac{1}{2}\right) = 3$$

[3 marks]

Question 11 continued

#### **METHOD 2**

adding $\Pi_l$ and $\Pi_2$ gives $4x - 2y = 5$	М1
given $y = \lambda \implies x = \frac{5}{4} + \frac{\lambda}{2}$	A1
$z = 2 - y - 3x = -\frac{7}{4} - \frac{5\lambda}{2}$	A1
$\Rightarrow \mathbf{r} = \begin{pmatrix} \frac{5}{4} \\ 0 \\ -\frac{7}{4} \end{pmatrix} + \lambda \begin{pmatrix} \frac{1}{2} \\ 1 \\ -\frac{5}{2} \end{pmatrix}$	AG

# [3 marks]

#### METHOD 3

$$n_{1} \times n_{2} = \begin{pmatrix} 2\\ 4\\ -10 \end{pmatrix}$$

$$= 4 \begin{pmatrix} \frac{1}{2}\\ 1\\ -\frac{5}{2} \end{pmatrix}$$
R1

common point 
$$\frac{5}{4} - 3(0) - \left(-\frac{7}{4}\right) = 3$$
 and  $-3\left(\frac{5}{4}\right) - 0 - \left(-\frac{7}{4}\right) = -2$  A1 [3 marks]

# (c) normal to $\varPi_3$ is perpendicular to direction of L

$$\Rightarrow \begin{pmatrix} a \\ b \\ c \end{pmatrix} \begin{pmatrix} 1 \\ 2 \\ -5 \end{pmatrix} = 0$$

$$\Rightarrow a + 2b - 5c = 0$$
A1
$$A1$$

$$[1 mark]$$

Question 11 continued

(d) (i) substituting 
$$\begin{pmatrix} \frac{5}{4} \\ 0 \\ -\frac{7}{4} \end{pmatrix}$$
 into  $\Pi_3$ :

$$\frac{5a}{4} - \frac{7c}{4} = 1$$

$$5a - 7c = 4 \qquad \qquad \textbf{AG}$$

attempt to find scalar products for  $\varPi_{\!\!1}$  and  $\varPi_{\!\!3},\,\varPi_{\!\!2}$  and  $\varPi_{\!\!3}$  and equating (ii)

and equating 
$$a-3b-c$$
 M1

$$\frac{ba^{2}+b^{2}+c^{2}}{\sqrt{11}\sqrt{a^{2}+b^{2}+c^{2}}} = \frac{a^{2}b^{2}-c^{2}}{\sqrt{11}\sqrt{a^{2}+b^{2}+c^{2}}}$$
M1

Note: Accept 
$$3a + b + c = a - 3b - c$$
.

  $\Rightarrow a + 2b + c = 0$ 

 attempt to solve  $a + 2b + c = 0$ ,  $a + 2b - 5c = 0$ ,  $5a - 7c = 4$ 

 M1

$$\Rightarrow a = \frac{4}{5}, b = -\frac{2}{5}, c = 0$$
 A1

hence equation is 
$$\frac{4x}{5} - \frac{2y}{5} = 1$$

for second equation:  

$$\frac{3a+b+c}{\sqrt{11}\sqrt{a^2+b^2+c^2}} = -\frac{a-3b-c}{\sqrt{11}\sqrt{a^2+b^2+c^2}}$$
(M1)  
 $\Rightarrow 2a-b=0$   
attempt to solve  $2a-b=0, a+2b-5c=0, 5a-7c=4$   
 $\Rightarrow a=-2, b=-4, c=-2$   
hence equation is  $-2x-4y-2z=1$ 

# [9 marks]

# Total [19 marks]